Unit 6 Quadratic Relations of the Form $y = ax^2 + bx + c$

Lesson Outline

BIG PICTURE

Students will:

- manipulate algebraic expressions, as needed to understand quadratic relations;
- identify characteristics of quadratic relations;
- solve problems by interpreting graphs of quadratic relations.

Day	Lesson Title	Math Learning Goals	Expectations
1	The <i>x</i> Tiles	 Connect the algebraic representations to the graphical representations of quadratics of the forms y = x² + bx + c and y = (x - r) (x - s). Expand and simplify second-degree polynomial expressions involving one variable that consist of the product of two binomials or the square of a binomial, using algebra tiles. 	QR1.01, QR2.04 CGE 4b, 5a
2	Multiply a Binomial by a Binomial Using a Variety of Methods	• Expand and simplify second-degree polynomial expressions involving one variable that consist of the product of two binomials or the square of a binomial, using the chart method, and the distributive property.	QR1.01, QR2.04 CGE 5a, 5b
3	Find the y-Intercept of Quadratic Equations	• Determine the connections between the <i>y</i> -intercept in the graph of a quadratic relation and the <i>c</i> in the algebraic form $y = x^2 + bx + c$, using technology.	QR1.01, QR2.04 CGE 3c, 5a
4	Finding x-Intercepts and Introduction to Factoring Quadratic Equations	 Determine the connections between the factored form of a quadratic relation and the <i>x</i>-intercepts of its graph. Factor simple trinomials of the form x² + bx + c, using a variety of tools, e.g., algebra tiles, paper and pencil, and patterning strategies. 	QR1.03, QR2.04 CGE 3c, 7b
5	Factoring Quadratic Relations of the Form $y = ax^2 + bx + c$, Where <i>a</i> Is a Common Factor	 Determine the connections between the factored form and the <i>x</i>-intercepts of a quadratic relation. Factor binomials and trinomials involving one variable up to degree two, by determining a common factor, using algebra tiles. 	QR1.02, QR2.04 CGE 5b
6	Use Intercepts to Graph Quadratic Equations	 Consolidate factoring. Connect factors to the <i>x</i>-intercepts of the graph of the quadratic relation. Graph quadratic relations, using intercepts. 	QR1.02, QR1.03, QR2.04 CGE 3c
7	We Have a Lot in Common	• Determine the connections between the factored form and the <i>x</i> -intercepts of the quadratic relation $y = x^2 + bx$.	QR1.03, QR2.04 CGE 3c, 5b
8	What's the Difference?	 Investigate the method of factoring a difference of two squares using patterning strategies and diagrams. Use the technique of factoring the difference of two squares to determine the <i>x</i>-intercepts of a quadratic relation. 	QR1.04, QR2.04 CGE 5b, 5e
9	Quick Sketches of Parabolas	• Use factoring techniques to find zeros and use understanding of the connection between the equation and the <i>y</i> -intercept and symmetry to make "quick" sketches of the related parabola.	QR1.02, QR1.03, QR1.04, QR2.04 CGE 5g

Day	Lesson Title	Math Learning Goals	Expectations
10, 11	Solve Problems Involving Quadratic Relations	• Solve problems involving quadratic relations by interpreting a given graph or a graph generated with technology from its equation.	QR3.01, QR3.02 CGE 5g
12	Summative Assessment	Note: A summative performance task is available from the members only section of the OAME web site <u>www.oame.on.ca</u>	
13	Jazz Day		

Unit 6: Day 1: The x Tiles

Grade 10 Applied

• BLM 6.1.1,6.1.2,

Materials

6.1.3

Math Learning Goals

- Connect the algebraic representations to the graphical representations of quadratics
 graphing calculators
 Expand and simplify second degree polynomial appressions involving one variable
 algebra tiles
- Expand and simplify second-degree polynomial expressions involving one variable that consist of the product of two binomials or the square of a binomial, using algebra tiles.

75 min

Minds On...

On... Whole Class → Demonstration

Toss a beach ball to a student. Ask the class to describe the path of the ball. Sketch the path of the ball on a graph with the independent axis representing horizontal distance from the teacher and the dependent axis representing height of the ball.

Draw another graph that represents the height of the ball over time (horizontal axis represents time, vertical axis represents the distance from the ground).

Lead a discussion that draws out the characteristics of the resulting parabola (symmetry, axis of symmetry, vertex, zeros, *x*-intercept, *y*-intercept).

Action! Pairs → Investigation

Provide the equation of the form $y = x^2 + bx + c$, in its standard and factored forms from BLM 6.1.1.

Students graph both forms, using a graphing calculator (BLM 6.1.2), to determine that they are the same graph and thus the same equation.

Whole Class → Gallery Tour

Post students' work: the two forms of the algebraic equation, a sketch of the graph, and a table of values. Students view the work of the other pairs. Debrief:

- What did you notice about the graphs?
- What did you notice about the tables of values?
- What can you infer about the two forms of the equations?

Whole Class → Modelling

- How do we get from one form to the other?
- What is the operation between the two sets of brackets?
- Demonstrate connection to multiplication of 20×12 , using base-ten materials.

Review algebra tiles: "1" tile (unit tile), x tile, and x^2 tile.

Using overhead algebra tiles, model the method of multiplying the factors to generate an area which represents the expanded form of the expression, e.g., $x^2 + 7x + 10$, $x^2 + 6x + 8$, $x^2 + 6x + 5$, $x^2 + 5x + 4$, using algebra tiles. Show the connection to multiplication of 20×12 , using base-ten materials.

Mathematical Process/Using Tools/Observation/Mental Note: Observe students' use of a graphing calculator to graph quadratic relations.

Consolidate Individual → Practice



Using algebra tiles, students multiply and simplify three examples with positive terms only.

y = (x + 4)(x + 3) y = (x + 2)(x + 5) y = (x + 3)(x + 2)

They make a sketch of the algebra tile solution.

Students check their answers on the graphing calculator by comparing the graphs of the two forms.

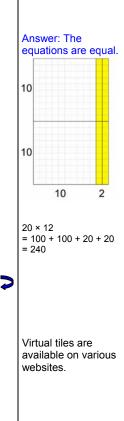
Home Activity or Further Classroom Consolidation

Practice

Complete the practice questions. Use worksheet 6.1.3 to show your solutions.

Assessment Opportunities





Provide appropriate practice questions for students.

6.1.1: Quadratic Equations (Teacher)

Standard Form	Factored Form
$y = x^2 + 3x + 2$	y = (x + 1)(x + 2)
$y = x^2 + 2x - 3$	y = (x - 1)(x + 3)
$y = x^2 - 1x - 6$	y = (x + 2)(x - 3)
$y = x^2 + x - 6$	y = (x - 2)(x + 3)
$y = x^2 + 5x + 4$	y = (x + 1)(x + 4)
$y = x^2 + 2x - 3$	y = (x + 3)(x - 1)
$y = x^2 - x - 6$	y = (x - 3)(x + 2)
$y = x^2 + 6x + 5$	y = (x + 1)(x + 5)
$y = x^2 - 4x - 5$	y = (x + 1)(x - 5)
$y = x^2 - 4x - 12$	y = (x + 2)(x - 6)
$y = x^2 + 6x + 8$	y = (x + 2)(x + 4)
$y = x^2 - 5x + 6$	y = (x - 3)(x - 2)
$y = x^2 - 2x - 3$	y = (x - 3)(x + 1)
$y = x^2 + 7x + 12$	y = (x + 3)(x + 4)
$y = x^2 + 7x + 10$	y = (x + 2)(x + 5)
$y = x^2 - 7x + 10$	y = (x - 2)(x - 5)

6.1.2: Graphing Quadratic Equations

Name:

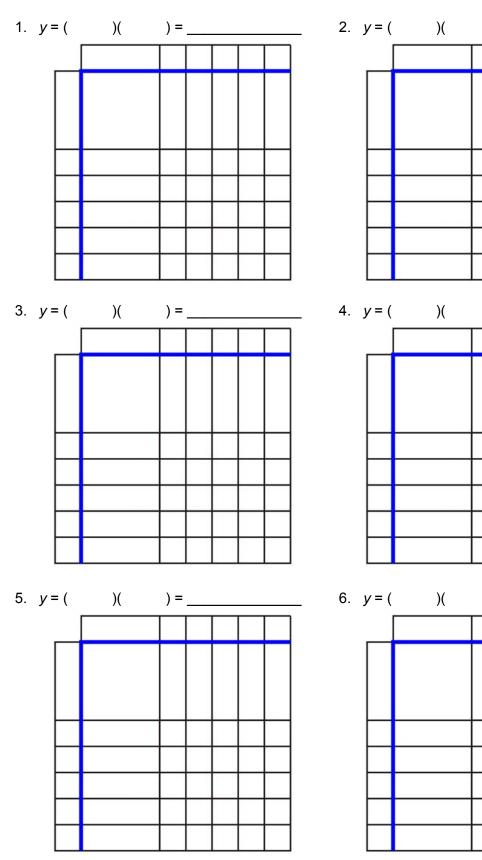
- 1. Obtain a pair of equations from your teacher.
- 2. Press the **Zoom** button and press **6** (for ZStandard) to set the window to make the max and min on both axes go from –10 to 10.
- 3. Press the y = button and key in your two equations into Y_1 and Y_2 .
- To change the graph of Y₂ to "animation": Move the cursor to the left of Y₂. Press Enter four times to toggle through different graph styles available.
 You should see ____()
- 5. Press **Graph**. First the Y_1 quadratic will appear, then the Y_2 quadratic will appear and be traced by an open circle.
- 6. Complete the three columns of the table below.

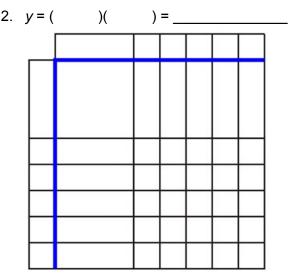
Our Two Equations	What They Look Like	What We Think It Means
	\uparrow	
	\downarrow	

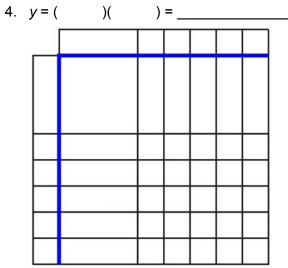
7. Press **2nd Graph** so that you can look at the tables of values for the two curves. Discuss what you see and complete the table.

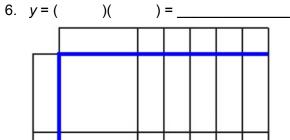
What We Noticed About the Table of Values	What We Think It Means

6.1.3: Algebra Tile Template

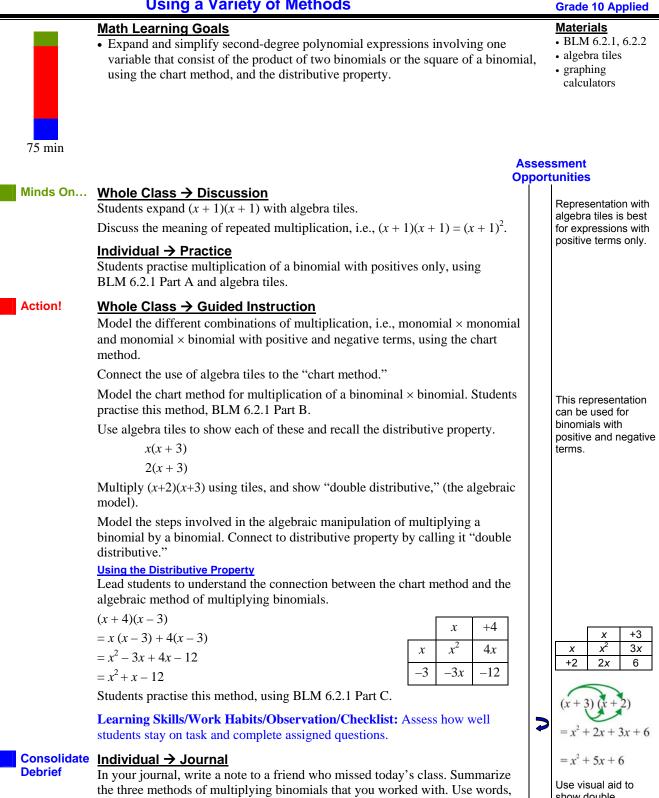








Unit 6: Day 2: Multiply a Binomial by a Binomial Using a Variety of Methods



show double distributive

Provide chart template 6.2.2 and algebra tile template 6.1.3, as needed.

Reflection

Home Activity or Further Classroom Consolidation

diagrams, and symbols in your explanation.

Solve the problems by multiplying the binomials.

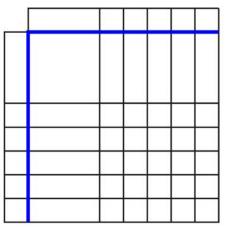
6.2.1: Multiply a Binomial by a Binomial

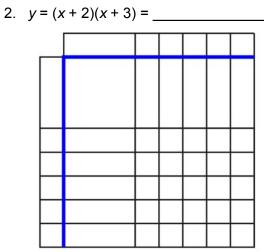
Name:

Part A

Use algebra tiles to multiply binomials and simplify the following:

1.
$$y = (x + 1)(x + 3) =$$

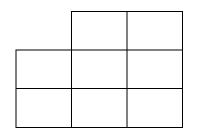




Part B

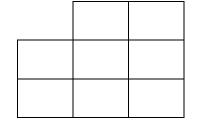
Use the chart method to multiply and simplify the following:

1.
$$y = (x + 1)(x + 3) =$$



2.
$$y = (x + 2)(x + 3) =$$

3.
$$y = (x + 2)(x - 1) =$$



5.
$$y = (x - 1)(x - 1) =$$

4.
$$y = (x-2)(x+3) =$$

6.
$$y = (x - 1)(x - 2) =$$

6.2.1: Multiply a Binomial by a Binomial (continued)

Part C

Multiply and simplify the two binomials, using the chart method and the distributive property.

1. $(x + 4)(x - 3)$	x +4 x -3	2. $(x-3)(x-3)$	x -3 x -3 -3
3. $(x+2)^2$	x +2 x +2	4. $(x+2)(x-1)$	x +2 x -1
5. (<i>x</i> – 2) (<i>x</i> + 1)	x -2 x +1	6. $(x-1)^2$	x -1 x -1 -1

7.	(<i>x</i> –	1)(<i>x</i> –	2)
----	--------------	----------------	----

	X	-1
x		
-2		
-		

8. (x-3)(x-4)

	X	-3
x		
-4		

6.2.1: Multiply a Binomial by a Binomial (continued)

Answers to Part B

1.
$$y = x^2 + 4x + 3$$

	x	1
x	<i>x</i> ²	x
3	3 <i>x</i>	3

4. $y = x^2 + x - 6$

7. $x^2 - 3x + 2$

_		x	-2
	x	x ²	-2 <i>x</i>
	3	3 <i>x</i>	-6

2. $y = x^2 + 5x + 6$ 3. $y = x^2 + x - 2$

	x	2
x	<i>x</i> ²	2 <i>x</i>
3	3 <i>x</i>	6

5. $y = x^2 - 2x + 1$

Х -1

х **x**²

-*x*

-1

-*x*

1

8. $x^2 - 7x + 12$

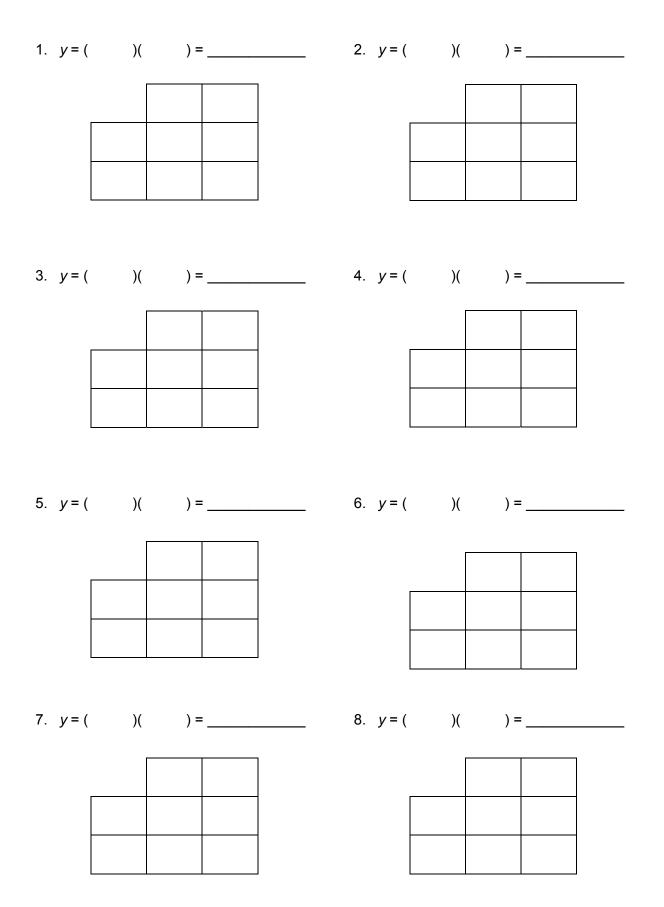
	x	2
x	<i>x</i> ²	2 <i>x</i>
-1	-x	-2

6. $y = x^2 - 3x + 2$

	x	-1
x	x ²	- <i>x</i>
-2	-2 <i>x</i>	2

Answers to Part C	
1. $x^2 + x - 12$	2. $x^2 - 6x + 9$
3. $x^2 + 4x + 4$	4. $x^2 + x - 2$
5. $x^2 - x - 2$	6. $x^2 - 2x + 1$

6.2.2: Chart Template for Distributive Property



Unit 6: Day 3: Find the y-Intercept of Quadratic Equations

Grade 10 Applied

Math Learning Goals	Materials
• Determine the connections between the <i>y</i> -intercept in the graph of a quadratic relation and the <i>c</i> in the algebraic form $y = x^2 + bx + c$, using technology.	 graphing calculators BLM 6.3.1, 6.3.2

75 min

75 11111		Asses	sment
_		Opport	unities
Minds On	Whole Class \rightarrow Modelling Pair students, and assign a person A and person B. Ask: What is meant by th <i>y</i> -intercept of a graph? A answers B. Ask: When we studied linear equations looked at $y = 3x + 2$. What did the 2 represent? B answers A. Explain the value of knowing the <i>y</i> -intercept for graphing.		
	Mathematical Processes/Communicating/Observation/Mental Note: Circulate as students work in pairs to note their use of mathematical languag	e.	
Action!	Pairs → Guided Investigation Pairs complete BLM 6.3.1 to identify the y-intercept of quadratic relations gin standard form and factored form.	ven	
Consolidate Debrief	Whole Class \rightarrow Summarizing Students summarize how the <i>y</i> -intercept of the graph relates to the equation of linear relations and quadratic relations, including why it is valuable to know <i>y</i> -intercept for graphing. Connect to the understanding that the <i>y</i> -intercept occurs when $x = 0$ for any relation, referring to algebraic and graphical forms during the discussions.		
Practice	Home Activity or Further Classroom Consolidation Complete worksheet 6.3.2.		Provide algebra tiles template 6.1.3 or chart template 6.2.2, as needed.

6.3.1: Finding the y-Intercept of a Quadratic Equation

Name:

1. Use the graphing calculator to find the *y*-intercept for each of the equations:

Equation	y-intercept
$y=x^2-x-2$	
$y = x^2 + 2x - 8$	
$y = x^2 - x + 6$	
y = (x-1)(x-2)	
y = (x+4)(x+3)	
$y = (x+3)^2$	

Note any patterns you see.

- 2. How can you determine the y-intercept by looking at a quadratic equation?
- 3. Which form of the quadratic equation is easiest to use to determine the *y*-intercept? Explain your choice.
- 4. Using your conclusion from question 2, state the *y*-intercept of each and check using a graphing calculator.

Equation	y-intercept	Does it check?		
Equation		Yes	No	
$y = x^2 - 2x - 8$				
$y = x^2 - x - 6$				
$y = x^2 + 3x + 2$				
y = (x-4)(x-1)				
y = (x-2)(x+5)				

5. Explain the connection between the *y*-intercept and the value of *y* when x = 0.

6.3.2: Quadratic Equations

Name:

1. Find the *y*-intercept for each of the following quadratic equations given in factored form. Write the equations in standard form. Show your work.

a)
$$y = (x-5)(x+2)$$
 standard form:
=
b) $y = (x+4)(x-3)$ standard form:
=
c) $y = (x-4)^2$ standard form:
=
d) $y = (x+5)^2$ standard form:
=
y-intercept:
standard form:
y-intercept:
standard form:
y-intercept:

2. Find the *y*-intercept for each of the following quadratic equations:

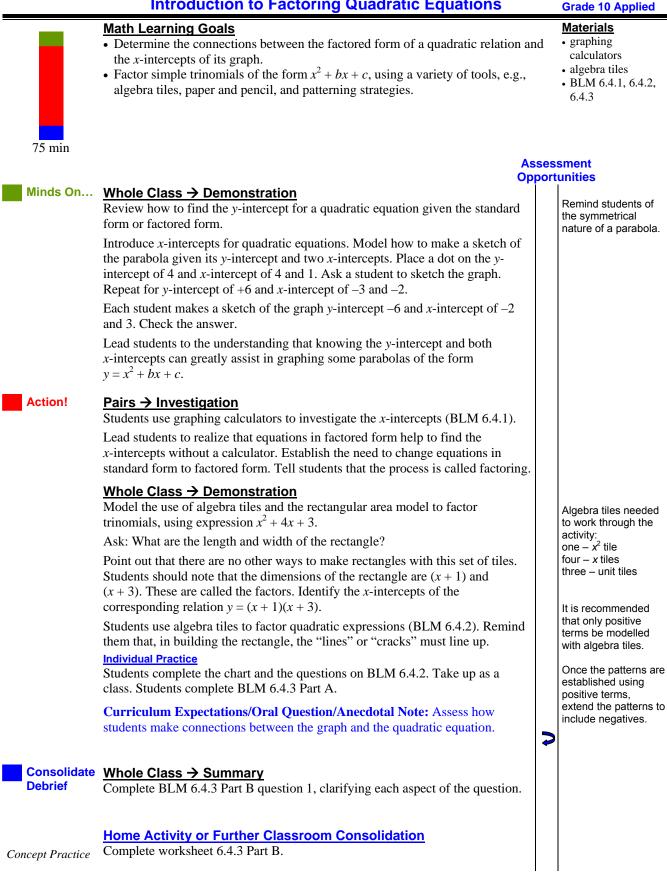
a)
$$y = (x+4)(x+2)$$

b) $y = (x-6)^2$

y-intercept:

y-intercept:

Unit 6: Day 4: Finding *x*-Intercepts and Introduction to Factoring Quadratic Equations



6.4.1: Finding the x-Intercepts of a Quadratic Equation

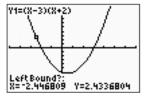
Name:

To find the x-intercepts:

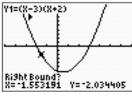
- 1. Enter the equation in Y₁. $y = x^2 x 6$
- 2. Press **ZOOM** and **6** (Zstandard) to set the scale for your graph. The calculator will then show the parabola.
- 3. Press **2nd TRACE** 1 to view the Calculate screen.



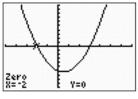
4. Select 2: ZERO. Your screen should be similar to the following screen.



5. You will be asked to enter a left bound. You can move the cursor to the left of one *x*-intercept (or just enter an *x* value that is to the left of the *x*-intercept). Press ENTER.



6. Repeat for the right bound, being sure that you are to the right of the same *x*-intercept.



- 7. The next screen will say guess. You can guess if you want but it is not necessary. Press ENTER. You will get one *x*-intercept.
- 8. Repeat steps 3 through 7 to get the other *x*-intercept.

6.4.1: Finding the x-Intercepts of a Quadratic Equation (continued)

Equation	First <i>x</i> -intercept	Second <i>x</i> -intercept
$y = x^2 - 4x - 12$		
$y = x^2 + 2x - 8$		
$y = x^2 - x + 6$		
y = (x-1)(x-2)		
y = (x+4)(x+3)		
y = (x-3)(x+5)		

1. Use the graphing calculator to find the *x*-intercepts for each of the following:

2. Can you determine the *x*-intercepts by looking at a quadratic equation? Explain.

3. Which form of the quadratic equation did you find the easiest to use when determining the *x*-intercepts? Explain the connection between the factors and the *x*-intercepts.

6.4.2: Area with Algebra Tiles

Name:

Using algebra tiles create the rectangles for the following areas. Complete the following chart.

Area of Rectangle	Number of <i>x</i> ² Tiles	Number of <i>x</i> Tiles	Number of Unit Tiles	Sketch of Rectangle	Length	Width
$x^2 + 4x + 3$						
$x^2 + 5x + 6$						
$x^2 + 6x + 8$						
x ² + 7x + 12						

1. Find a relationship between the number of *x* tiles and the numbers in the expressions for the length and width.

2. Find a relationship between the number of unit tiles and the numbers in the expressions for the length and width.

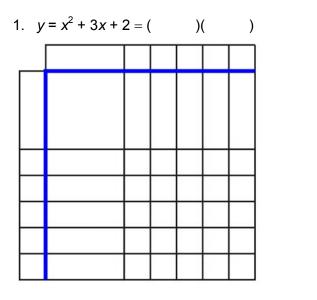
3. If the area of a rectangle is given by $x^2 + 8x + 15$, what expression will represent the length and the width?

6.4.3: Factoring Using Algebra Tiles and Making Connections to the Graphic

Name:

Part A

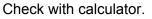
For each of the following, shade in the appropriate rectangular area. Then shade in the tiles that represent the length and width for each of those areas. Use the length and width to represent and state the factors. State the *x*-intercepts. Check using a graphing calculator.

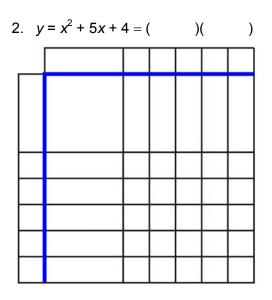


x-intercepts _____, ____

Check with calculator.

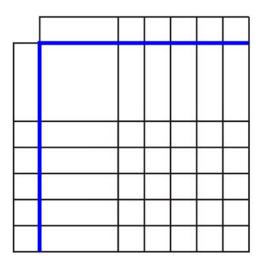
3. $y = x^2 + 6x + 5 = ()()$





x-intercepts _____, ____ Check with calculator.

4.
$$y = x^2 + 4x + 4 = ($$
)()



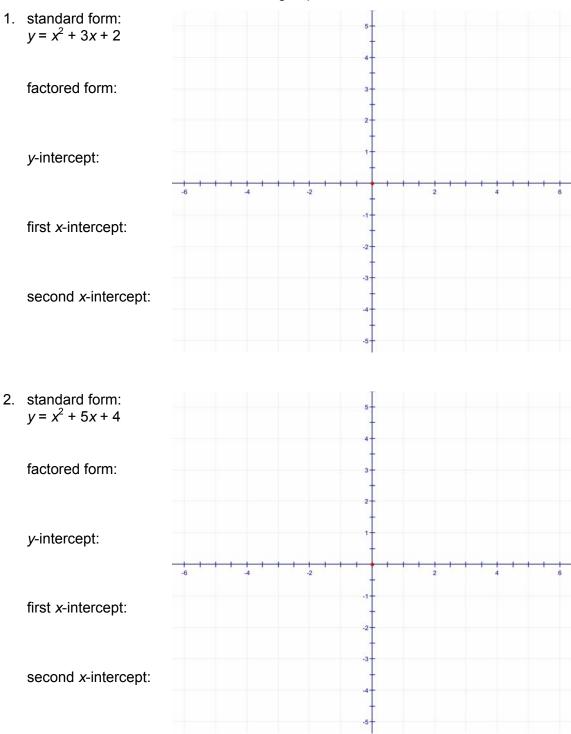
x-intercepts _____, ____

Check with calculator.

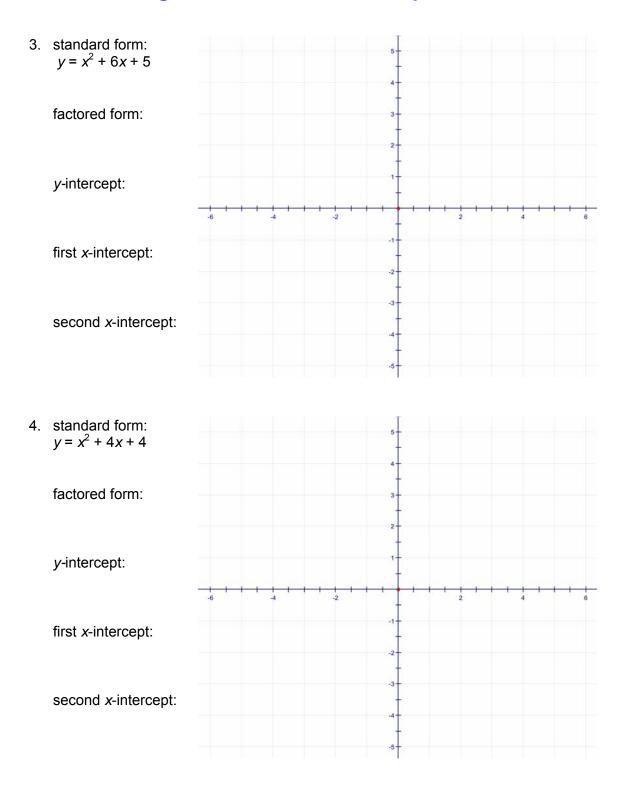
6.4.3: Factoring Using Algebra Tiles and Making Connections to the Graphic (continued)

Part B

Using the diagrams in Part A, find the *x*- and *y*-intercepts for each quadratic relation. Use the information to make the sketch on the grid provided.



6.4.3: Factoring Using Algebra Tiles and Making Connections to the Graphic (continued)



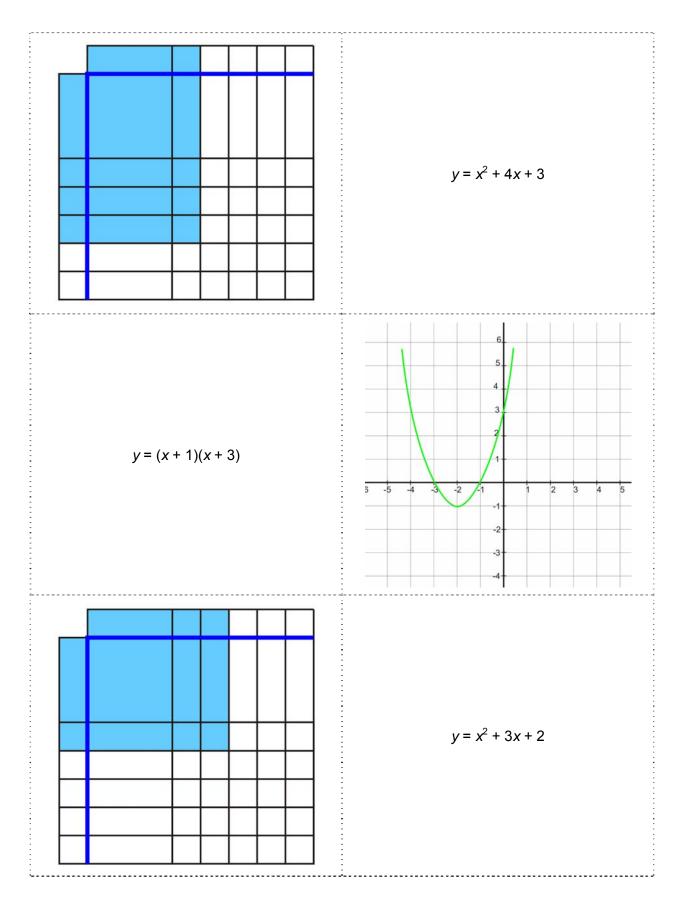
5. In what way is the last example different from the others?

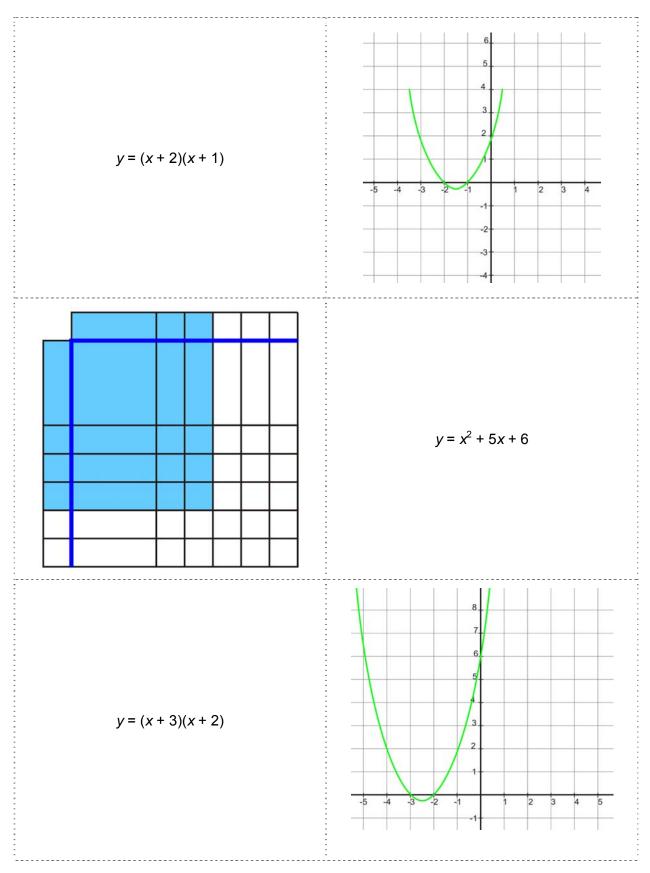
Unit 6: Day 5: Factoring Quadratic Relations of the Form $y = ax^2 + bx + c$, Where *a* is a Common Factor

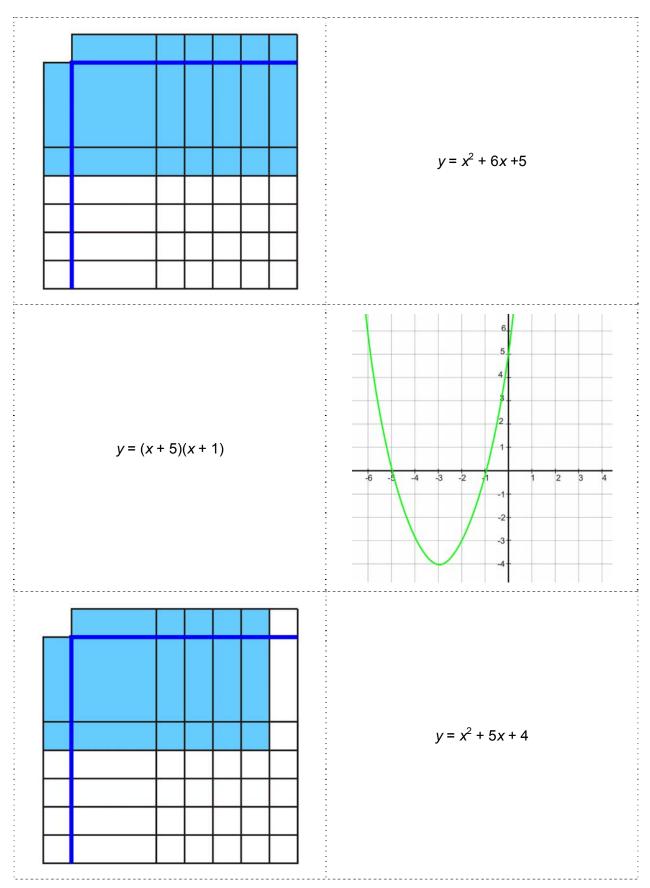
Grade 10 Applied

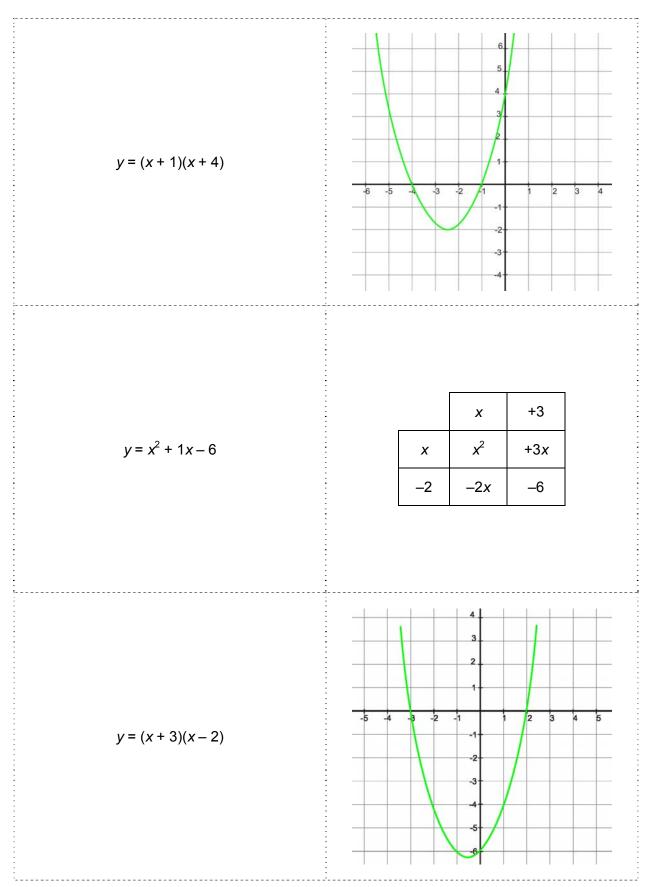
	Where a Is a Common Factor		Grade 10 Applied
75	 Math Learning Goals Determine the connections between the factored form and the <i>x</i>-intercepts of a quadratic relation. Factor binomials and trinomials involving one variable up to degree two, by determining a common factor using algebra tiles. 		Materials • algebra tiles • graphing calculators • BLM 6.5.1, 6.5.2, 6.5.3 • glue stick
75 min	Ass	ess	sment
Minda On		ortu	inities
Minds On	Review the forms of equations and representations of quadratics and label four stations: factored form, standard form, graphical form, and chart or algebra tiles representation. Randomly hand out the cards (BLM 6.5.1).		
	Students move to the corner for the form represented on their card and check that everyone has the same form. They can help one another express their representation in the other forms and jot them on the back of their cards. They then "find" the other three people holding the related cards.		
	Groups justify they all have different forms of representations of the same quadratic. Paste these on a single page and post them for a gallery walk.		
	Curriculum Expectations/Demonstration/Marking Scheme: Collect worksheets and assess students' understanding of the concepts needed to complete the Home Activity from Day 4.	2	
Action!	Pairs → Investigation		$r \times s = -6$
	Students complete BLM 6.5.2. Discuss the ideas investigated and extend to relations that include negative coefficients for <i>b</i> and <i>c</i> , e.g., $y = x^2 - x - 6$. Students should understand that $(r) \times (s) = c$ and $r + s = b$, yielding factors $(x + r)(x + s)$ and <i>x</i> -intercepts of $-r$ and $-s$.		r + s = -1 -3 and 2 factors are (x - 3)(x + 2) x intercepts 3 and -2
	Students complete BLM 6.5.3 and share their solutions on the overhead.		
	Whole Class → Guided Instruction		
	Introduce common factoring by displaying overhead tiles for $3x + 3$. Demonstrate that this is 3 groups of $(x + 1)$, thus this can be expressed as $3(x + 1)$. The "common factor" is 3. Repeat for $2x + 4$ and $5x - 10$. Display the overhead tiles needed to factor $2x^2 + 2x + 2$.		In Grade 10 Applied, students only factor $ax^2 + bx + c$ when a is a common factor.
	Ask:Can these be placed into groups where each type of tile is equally represented in all groups? Why or why not?How many groups did you get? What are the contents of each group?		Answer: $y = 2x^2 + 2x + 2$ $y = 2(x^2 + x + 1)$ i.e., 2 sets of
	Show how the factored answer would be expressed. Complete several more examples, such as: $3x^2 + 6x + 12$, $2x^2 + 6x - 8$, $2x^2 - 8x + 10$, $4x^2 + 8x + 8$.		$x^2 + x + 1$
	For $4x^2 + 8x + 8$, some students may think that 2 groups of $(2x^2 + 4x + 4)$ would be appropriate when 4 groups of $(x^2 + 2x + 2)$ is the most appropriate answer. Use this example to discuss the greatest common factor.		Another similar example: $y = 4x^2 + 12x + 12$
Consolidate Debrief	Individual \rightarrow Journal Students summarize how to factor a trinomial, including conditions that make it possible for a trinomial to be factored and how to determine a common factor.		
Concept Practice	Home Activity or Further Classroom Consolidation Complete the practice questions.		Provide questions that require checking answers by expanding or graphing with technology.

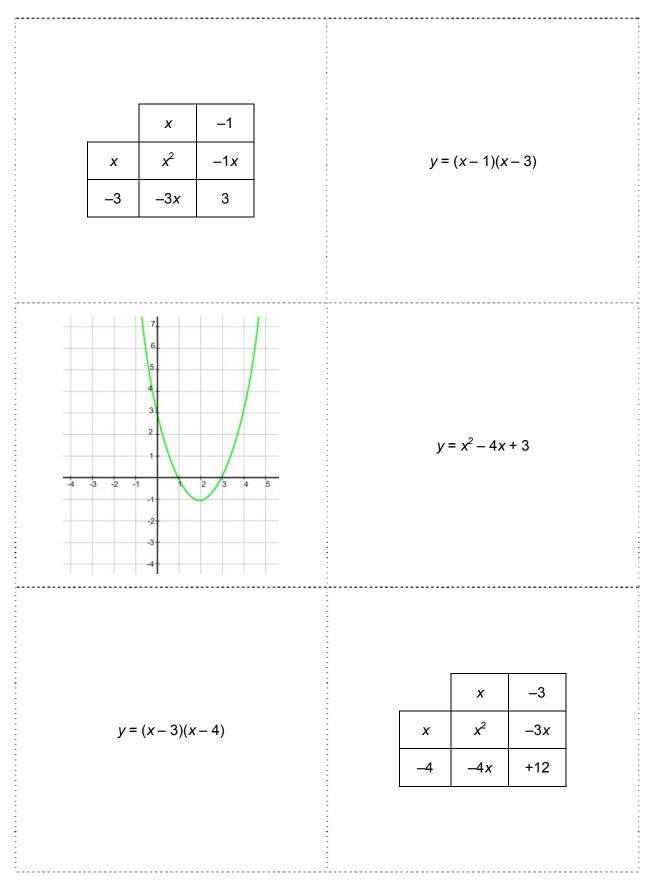
6.5.1: Four Corners

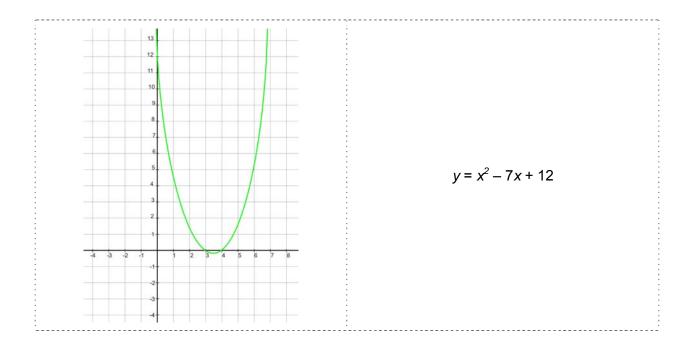












6.5.2: Factored Form and x-Intercepts

Name:

Use algebra tiles to find the length and width for each given area. Use the graphing calculator to find the *x*-intercepts of the corresponding quadratic relation. Graph both the area model and factored form of the quadratic relation to check that these are the same before finding the *x*-intercepts.

Area	Length	Width	Factored Form	First <i>x</i> -intercept of corresponding relation	Second <i>x</i> -intercept of corresponding relation
$x^2 + 4x + 3$					
$x^2 + 5x + 6$					
$x^2 + 6x + 8$					
$x^2 + 7x + 12$					

- 1. What do you notice about the constant term in the length and width expressions and the coefficient of the *x* term in the area expressions?
- 2. What do you notice about the constant term in the length and width expressions and the constant term in the area expressions?
- 3. If an area is expressed as $x^2 + 10x + 21$, what must be true of the constant terms in the length and width expressions?
- 4. If the standard form of a quadratic relation is $y = x^2 + bx + c$, and it has *x*-intercepts of *r* and *s*, then the same relation would then be y = (x r)(x s). How would you find the value of *r* and *s*?

6.5.3: Match It!

Name:

Match each pair of numbers on the left with the correct product and sum on the right.

	Pair of Numbers		Product and Sum
1.	r = −1, s = −5	a.	r × s = 5 r + s = 6
2.	<i>r</i> = 1, s = 6	b.	$r \times s = -5$ $r + s = -4$
3.	<i>r</i> = 2, <i>s</i> = −3	C.	r × s = -5 r + s = 4
4.	<i>r</i> = 1, <i>s</i> = –5	d.	r × s = 5 r + s = -6
5.	<i>r</i> = −3, <i>s</i> = 4	e.	r × s = 6 r + s = 7
6.	r = −1, s = 5	f.	$r \times s = 6$ $r + s = -7$
7.	<i>r</i> = –6, <i>s</i> = 2	g.	$r \times s = -6$ r + s = -1
8.	<i>r</i> = 1, <i>s</i> = 5	h.	$r \times s = 12$ r + s = 13
9.	<i>r</i> = −1, <i>s</i> = −6	i.	r × s = -12 r + s = -4
10.	r = 1, s = 12	j.	r × s = -12 r + s = 1

Unit 6: Day 6: Use Intercepts to Graph Quadratic Relations

Grade 10 Applied

Materials

- BLM 6.6.1
- large chart (grid) paper



Action!

Math Learning Goals • Consolidate factoring. • Connect factors to the *x*-intercepts of the graph of the quadratic relation. • Graph quadratic relations, using intercepts. Minds On... Pairs \rightarrow Review Students discuss their journal entry from Day 5 and refer to their answers on BLM 6.5.1 and 6.5.2.

of the corresponding relation:

Assessment **Opportunities**

Pairs factor the following quadratic expressions, discuss what is the same and different about each, and how the results would correspond to the x-intercepts Curriculum Expectation/Observation/Checklist: Listen to students' ~ conversations to identify level of understanding of factoring trinomials and the Include some examples where the parabola is opening downward, and where there is a double root. Note the use of the word sketch. The graph is not intended to be exact, but to show the symmetry, the intercepts, and the general movement of the curve. Students can visualize and draw their solution in the air also. Some students may still need algebra tiles to factor. Students check their answers using the response on the overhead and on the Lead a discussion that compares graphing linear relations using intercepts and quadratic relations using intercepts. Discuss how factoring provides an efficient

Home Activity or Further Classroom Consolidation

Differentiated Exploration Reflection

Consolidate

Debrief

Complete the practice questions.

Provide students with appropriate practice questions.

Whole Class → Demonstration	

 $x^{2} + 11x + 30$, $x^{2} - 11x + 30$, $x^{2} - x - 30$, $x^{2} + x - 30$.

connection between the factors and the *x*-intercepts.

Using large chart (grid) paper, place a dot on the x-axis at -4 and 2, and a dot on the y-axis at -8. Point out the -4 and 2 are the x-intercepts and -8 is the y-intercept of a parabola.

Ask volunteers to sketch the parabola that goes through these points. Point out that, at this time, they are focusing on the symmetry of the parabola, and that the parabola intersects correctly on the y-axis, and the x-axis. Repeat this several times using other values for the intercepts.

Discuss question A on BLM 6.6.1 and do question B together. Refer to question F to be sure students understand what is different in this question.

Individual → Practice

Students complete BLM 6.6.1.

Whole Class → Discussion

chart paper grid.

Students who finish early can assist students who are having difficulty, and/or put an answer on the overhead and make a sketch of the relation on large chart (grid) paper.

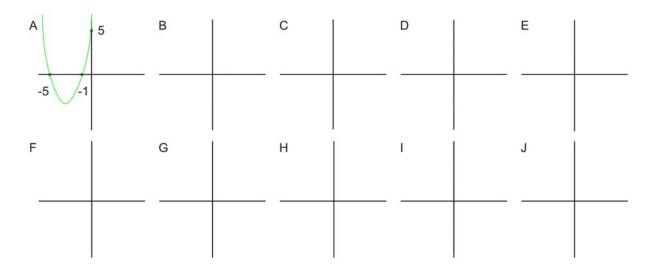
method for making a sketch of the graph, recognizing that it is a sketch only.

6.6.1: Use Intercepts to Graph It!

Given the standard form of the quadratic relation, identify the value of the sum and product needed to factor. Express the relation in factored form, identify the *x*-intercepts and *y*-intercept, and use these results to make a sketch of each parabola.

	Standard Form	Product and Sum	Pair of Numbers	Factored Form	<i>x</i> -intercepts	y-intercept
Α	$y = x^2 + 6x + 5$	r × s = 5 r + s = 6	r = 1, s = 5	y = (x+1)(x+5)	–1 and –5	5
в	$y = x^2 - 4x - 5$	r × s = –5 r + s = –4				
С	$y = x^2 + 4x - 5$	r × s = –5 r + s = 4				
D	$y = x^2 - 6x + 5$	r×s=5 r+s=–6				
Е	$y = x^2 + 7x + 6$	r × s = 6 r + s = 7				
F	$y = x^2 - 6x + 9$	r × s = r + s =				
G	$y = x^2 - x - 6$	r × s = r + s =				
н	$y = x^2 + 13x + 12$	r × s = r + s =				
I	$y = x^2 - 4x - 12$	r × s = r + s =				
J	$y = x^2 + x - 12$	r × s = r + s =				

Sketch of the relation



6.6.1: Use Intercepts to Graph It! (Answers)

	Standard Form	Product and Sum	Pair of Numbers	Factored Form	<i>x</i> -intercepts	y-intercept
A	$y = x^2 + 6x + 5$	r×s=5 r+s=6	r = 1 s = 5	y = (x+1)(x+5)	–1 and –5	5
в	$y=x^2-4x-5$	r × s = -5 r + s = -4	r = 1 s = -5	y = (x+1)(x-5)	–1 and 5	-5
с	$y = x^2 + 4x - 5$	r × s = –5 r + s = 4	r = -1 s = 5	y = (x-1)(x+5)	1 and –5	-5
D	$y = x^2 - 6x + 5$	r × s = 5 r + s = -6	r = -1 s = -5	y = (x-1)(x-5)	1 and 5	5
Е	$y = x^2 + 7x + 6$	r×s=6 r+s=7	r = 1 s = 6	y = (x+1)(x+6)	–1 and –6	6
F	$y = x^2 - 6x + 9$	r × s = 9 r + s = -6	r = -3 s = -3	y = (x-3)(x-3)	3	9
G	$y=x^2-x-6$	r × s = –6 r + s = –1	r = 2 s = -3	y=(x+2)(x-3)	–2 and 3	-6
н	$y = x^2 + 13x + 12$	r × s = 12 r + s = 13	r = 1 s = 12	y = (x+1)(x+12)	–1 and –12	12
I	$y = x^2 - 4x - 12$	r × s = –12 r + s = –4	r =6 s = 2	y=(x-6)(x+2)	6 and –2	-12
J	$y = x^2 + x - 12$	r×s=–12 r+s=1	r = -3 s = 4	y = (x-3)(x+4)	3 and –4	-12

Unit 6: Day 7: We Have a Lot in Common

Math Learning Goals

quadratic relations $y = x^2 + bx$.

Grade 10 Applied

<u>Materials</u>

- graphing
- calculators
- algebra tiles
- overhead algebra
- tiles
- BLM 6.7.1, 6.7.2,
- 6.7.3

Answers

Same: zero as a y-intercept, zero as

one x-intercept.

shape, and size,

Different: the other

opening up

x-intercept

 \supset

Assessment Opportunities

75 min

Action!

Minds On... Whole Class → Discussion

Use the context of kicking a soccer ball. Depending on the kick, the ball may travel different heights and distances. Lead a discussion as to how to draw a height vs. horizontal distance graph for three scenarios in which there are different height and distance measures.

• Determine the connections between the factored form and the x-intercepts of the

Ask:

- If you were to represent this scenario graphically:
 - what are appropriate labels for the axes? [height above ground in metres; horizontal distance from the kicker's toe in metres]
 - where would the point be that represents the kick?
 - what would one of the *x*-intercepts of the graph be?
 - what might the general equation of the graph look like?

Pairs → Group Investigation

Students work through the graphing calculator investigation (BLM 6.7.1).

Provide each pair with one of the following equations: $y = x^2 + 4x$, $y = x^2 + 6x$, $y = x^2 - 2x$, $y = x^2 - 5x$. Pairs of students complete questions 1–3 on BLM 6.7.1.

Form groups of four where each student in the group has a different equation. Students complete questions 4–9 (BLM 6.7.1). They compare what is the same about their graphs and what is different and comment on the *x*-intercept, *y*-intercept, and the general shape. Lead a discussion about the algebraic representations, e.g., y = x (x + 4), y = (x - 0)(x + 4) and y = (x + 4)(x - 0) being equivalent ways of expressing the equation $y = x^2 + 4x$ in factored form.

Use algebra tiles to demonstrate common factoring of $y = x^2 + 6x$, then do Example 1 and 2 of BLM 6.7.2. Students complete BLM 6.7.2. (See Teacher BLM 6.7.3.)

Mathematical Process/Using Tools/Observation/Anecdotal Note: Assess students' use of graphing calculators and algebra tiles to identify the factors.

Whole Class → Demonstration

Relate the algebra tile method of factoring to the algebraic method. Demonstrate the algebraic method using several examples, including some with negatives.

Consolidate Individual → Journal Debrief Students describe the thr

Students describe the three methods of common factoring that were investigated in the lesson, and describe the connections of the factors to the *x*-intercepts of the corresponding relation.

Home Activity or Further Classroom Consolidation

Concept Practice

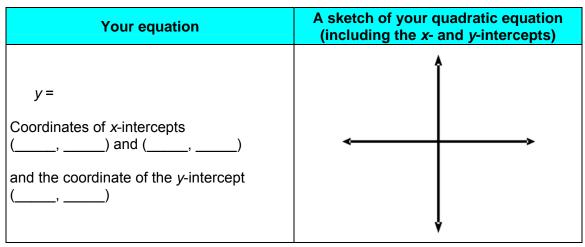
Complete the practice questions.

Provide students with appropriate practice questions.

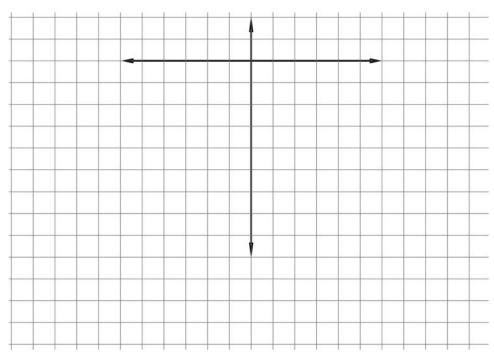
6.7.1: Investigate Relations of the Form $y = ax^2 + b$

Name:

- 1. Obtain a graphing calculator and equation from your teacher.
- 2. Type in the equation (using the **Y** = button on your calculator). Key in **zoom 6** to get the max and min from –10 to 10 on your window.
- 3. Fill in the table.



4. In your group, sketch all four graphs.



5. Identify what is the same and what is different in these four graphs.

6.7.1: Investigate Relations of the Form $y = ax^2 + b$ (continued)

6. Fill in the following table.

Standard form	From the graph, identify the <i>x</i> -intercepts <i>r</i> and <i>s</i>	Write each equation in factored form y = (x - r)(x - s)
$y = x^2 + 4x$	r = s =	
$y = x^2 + 6x$	r = s =	
$y = x^2 - 2x$	r = s =	
$y = x^2 - 5x$	r = s =	

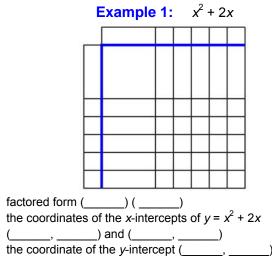
- Clear the y = screen on one of the four calculators, enter the factored form of the four equations, and graph. Are these graphs the same as the ones in your sketch?
 If yes, continue to question 8. If no, revise and check. Ask your teacher for assistance, if needed.
- 8. Can the equations in the third column of your table be simplified? Explain.

9. Record the simplified versions of your relation in factored form.

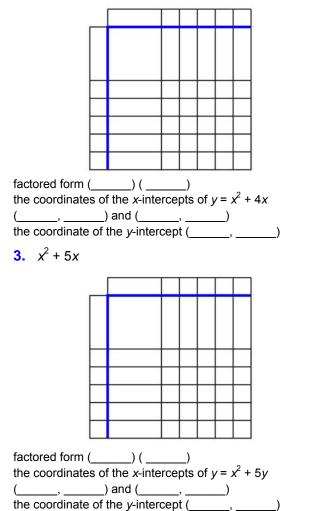
Standard Form	Factored Form
$y = x^2 + 4x$	
$y = x^2 + 6x$	
$y = x^2 - 2x$	
$y = x^2 - 5x$	

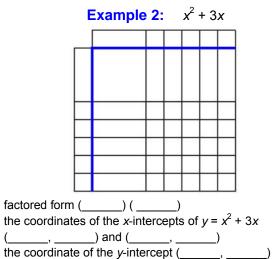
6.7.2: Factoring $x^2 + bx$

Consider the outer portion of the algebra tile representation as the length and width of a room. The rectangle is the carpet. Colour in as many cells as required for each example to form a rectangle. To factor, form a rectangle using the tiles, then determine the length and width of the room.

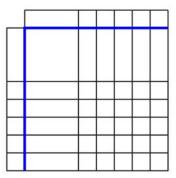


Use your algebra tiles to factor the following: 1. $x^2 + 4x$





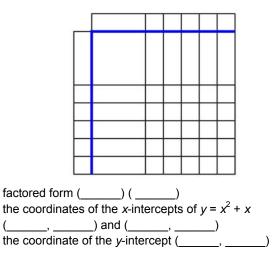




factored form () () the coordinates of the *x*-intercepts of $y = x^2 + 1x$ (_____, ____) and (_____, ____) the coordinate of the y-intercept (



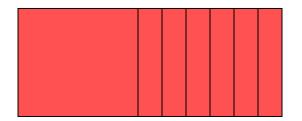
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6.7.3: Two Methods for Factoring $x^2 + bx$ - Teacher

1. Algebra Tile Model for Common Factoring

Use overhead tiles to demonstrate the concept of common factoring for the example $x^2 + 6x$.

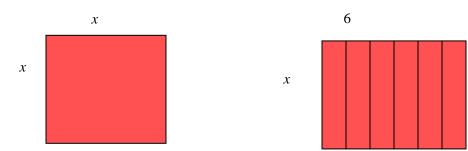


Explanation

This is the only rectangle that can be formed with algebra tiles. Factoring requires identifying the length and the width that results in this rectangle's area. In this case the dimensions are (x) and (x + 6).

Alternative Explanation

Separate the x^2 tile from the x tiles to show the length and width of each part of the expression.



In the square, the area is given by x times x. In the rectangle, the area is given by x times 6. The total area is given by (x)(x) + (x)(6), we say that x is a common factor of each term.

Explain

x multiplies x, and x multiplies 6, thus x multiplies x and 6; that is, x multiplies (x + 6), or x (x + 6)

Repeat the process with $x^2 + 3x$.

2. Algebraic Model for Common Factoring

Use the principle of what is common to each term to factor the right-hand side of each equation. Lead the class through algebraic thinking in factoring the following examples:

$$x^2 - 1x$$
 $x^2 + 5x$ $x^2 - 2x$

= x (x-1) = x (x+5) = x (x-2)

Day 8	3: What's the Difference?		Grade 10 Applied
	 Math Learning Goals Investigate the method of factoring a difference of two squares using patterning strategies and diagrams. Use the technique of factoring the difference of two squares to determine the <i>x</i>-intercepts of a quadratic relation. 		Materials • graphing calculators • BLM 6.8.1
75 min			
			ment nities
Minds On	Individual \rightarrow Reflection Students reflect on the connection between $x^2 - 36$, $y = x^2 - 36$, and the corresponding graph. They fold a paper into thirds and write the headings " I Think, I Wonder, I Know " in the columns. Students complete the first and second columns, and share their reflection with a partner.		
	Math Process/Communicating/Observation/Anecdotal Note: Assess students' use of mathematical language related to quadratic relations.	>	
Action!	Pairs-> Investigation Students use a graphing calculator to identify the intercepts of quadratic relations of the form $y = x^2 - a^2$ and connect the <i>x</i> -intercepts to the factors (BLM 6.8.1).		
	Circulate to clear any misconceptions and to guide pairs, as needed. Whole Class \rightarrow Guided Instruction Activate students' prior knowledge by factoring the relation $y = x^2 + 7x + 12$. $3 \times 4 = 12, 3 + 4 = 7$. Therefore $y = x^2 + 7x + 12$ can be expressed in factored form as follows: $y = (x + 3)(x + 4)$		The shaded area $x^2 - 49$. You can see the two
	Ask how $y = x^2 - 49$ could be written as a trinomial. [Answer: $y = x^2 + 0x - 49$] Model the process: $(+7)(-7) = -49$ and $(+7) + (-7) = 0$		squares and the shaded area is the difference betwee their areas. When we factor, we wan
	Therefore, $y = x^2 - 49$ can be expressed in factored form as $y = (x + 7)(x - 7)$. Reinforce the fact that the <i>bx</i> term is 0 <i>x</i> and thus is not written in the expression. (Zero times <i>x</i> is zero.)		to find length and width of the rectangle having this area.
	Explain why this type of quadratic is called a "difference of perfect squares," illustrating both algebraically and pictorially. Students practise solving problems involving factoring a difference of squares.		
			$\downarrow \qquad \qquad$
Consolidate Debrief	<u>Whole Class → Discussion</u> Students complete the third column in their "I Think, I Wonder, I Know" chart.		t → x+7 x → 1
	Review factoring a difference of squares and its connection to the graph, as needed.		The length is $x + 1$
	Home Activity or Further Classroom Consolidation		and width is $x - 7$

Practice

Home Activity or Further Classroom Consolidation Practise factoring and connecting the factors to the graph.

TIPS4RM: Grade 10 Applied: Unit 6 – Quadratic Relations of the Form $y = ax^2 + bx + c$ (August 2008)

6.8.1: Graphing Relationships of the Form $y = x^2 - a^2$

Name:

 Working with a partner and one graphing calculator, set your Window: Xmin = -10; Xmax = 10; Xscl = 1; Ymin = -36; Ymax = 10; Yscl = 1; Xres = 1.

Complete the following table.

	Relation in standard form	Sketch each graph. Label as A, B, C, D, or use different colours.	<i>y</i> - intercept	x- intercept (r)	x- intercept (s)	Relation in factored form y = (x - r) (x - s)
A	$y = x^2 - 4$					
в	$y = x^2 - 9$					
С	$y = x^2 - 16$	-5 -4 -3 -2 -1 1 2 3 4 5 -5 -4 -3 -2 -1 -5 				
D	$y = x^2 - 25$					

Consider your results from question 1 and answer the following questions.

- 2. What is the same about the relations?
- 3. What is the same about the graphs?
- 4. What is the same about the vertex of each graph?
- 5. What do you notice about the *r* and *s* values of each relation?
- 6. Solve this puzzle. How can you find the y-intercept and the x-intercepts of the graph of a quadratic relation of the form $y = x^2 a^2$?

Unit 6 Day 9	: Quick Sketches of Parabolas	Grade 10 Applied
Minds On: 15 M Action: 45 M Consolidate/ Debrief: 15 M Total = 75 Min	• Use factoring techniques to find zeros and use understanding of the connection between the equation and the y-intercept and symmetry to make "quick" sketches of the related parabola, given $y = x^2 + bx + c$	Materials - graphing calculators - BLM 6.9.1 - BLM 6.9.2 - BLM 6.9.3 - BLM 6.9.4
		ment unities
Minds On	Whole Class – ReviewReview the key characteristics of a parabola (vertex, symmetry, y-intercept, zeros).Review values in standard form of a parabola (a, b, c) and how that connects to the graph.Review how to factor a trinomial (from standard form to factored form).	Use diagrams, descriptions, equations and draw connecting arrows between the various forms.
Action!	Whole Class - DiscussionDistribute BLM 6.9.1 to class. Review the first and third questions and allow students time to do the second and fourth questions. Go over work and correct any misconceptions and errors.Curriculum Expectation/Oral Questions/Observation/Mental Note: Take up the first and third questions verbally and then observe how students demonstrate their understanding of factoring and graphing.Individually - Activity Distribute BLM 6.9.2 to students. They should work individually on matching equations from column A (standard form) to column B (factored form).	Performance Task or can be used as a Quiz or Observation
Consolidate Debrief	Pairs – Think, Pair, ShareDistribute BLM 6.9.3 – Each student graphs the equations shown. Whenfinished, each student pairs up with one other student and compares graphsand the process they used to make them.Mathematical Process/Communication/Oral Questions: Observe studentsas they graph the equations. Pose questions. Observe students explainingand sharing with others.	
Concept Practice	Home Activity or Further Classroom Consolidation Provide students with appropriate practice questions.	Consider providing students with a chart template like 6.9.1 to organize

6.9.1 Quick Review of Factoring and Graphing

For each of the following:

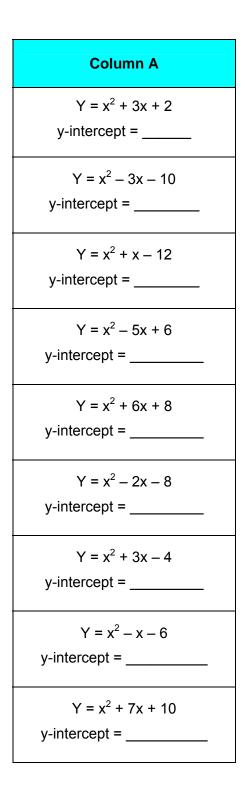
- identify what information the equation tells you about the parabola
- factor the equation and identify what the new form of the equation tells you
- sketch the parabola using the information you have (make sure you plot key points!)

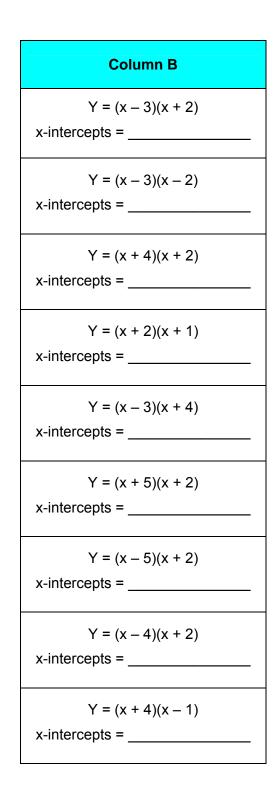
Equation (Standard Form)	Y- Intercept	Factored Form	Zeros	Sketched Graph
1. $y = x^2 - 7x + 10$				
2. $y = x^2 - x - 6$				

Zeros	Standard Form	Y- Intercept	Sketched Graph

6.9.2 Matching

- For each equation in column A, state the y-intercept.
- For each equation in column B, state the zeros (or x-intercepts)
- Each equation in column A has a matching equation in column B. Draw an arrow



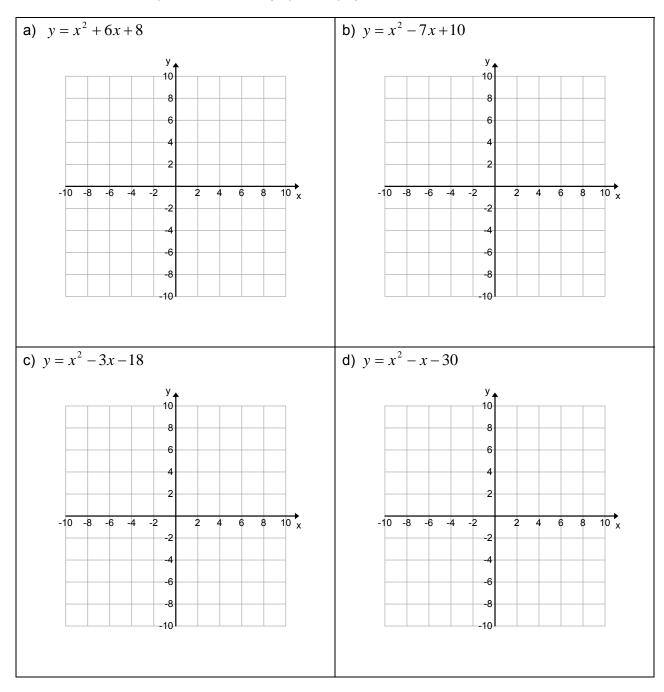


6.9.3 Quick Sketches of Parabolas

For each quadratic function given below determine:

- The zeros (*x*-intercepts)
- The y-intercept

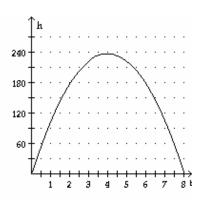
With the information you find and using symmetry, graph each parabola.



Unit 6 Day 10	: Applying Quadratic Relationships		Grade 10 Applied
Minds On: 15 M Action: 50 M Consolidate/ Debrief: 10 M Total = 75 Min	 Solve problems involving quadratic relations by interpreting a given graph or a graph generated with technology from its equation. 	1	Materials • graphing calculator • overhead projector/screen • graphing calculator screen • BLM 6.10.1 • BLM 6.10.2
			ment
Minds On		ort	unities Clearing Data
Minds On	<u>Whole Class – Demonstration</u> Review graphing calculator functions for graphing quadratics.		Graphing Data Graphing Equations Setting Window limits
	BLM 6.10.1- Go through two basic problems with the class. Highlight what they need to think about as they dissect a problem and relate it to what they know about quadratics.	1	Vertex, Zeros, etc.
Action!	Individual – Activity	Q	
	Distribute BLM 6.10.2 and review the instructions – Students complete the first question individually while teacher walks around to monitor progress. Mathematical Process/Connecting/Observation/Mental Note: Observation to see if students are applying skills to basic real-life situations.		
	Pairs – Activity BLM 6.10.2 – Students should complete second question in pairs. Encourage discussion to assist decision making and problem solving process.		Could be used as a Performance Task
Consolidate Debrief	 Whole Class –Reflection/Organizer Wrap up questions for students to answer and make note of, for example: What do the zeros represent in a real life situation? What can the vertex tell us? What has the y-intercept represented? Give students a graph and have them create questions about it that would show they can analyze the graph. If time permits, have students exchange their graphs and graptions and practice answering the questions. 		Oral Questions – ensure students have made the connection between the parabola and its real-life meaning
Application Concept Practice	their graphs and questions and practice answering the questions. Home Activity or Further Classroom Consolidation Provide students with appropriate practice questions.		теание теаниц

6.10.1 Problem Solving with Quadratic Graphs-Interpreting Parabolas

- The graph below shows the height, in meters, of a diver jumping off a springboard versus time, in seconds.
 - a) What is the initial height of the jumper? _____
 What is this called in math terminology?
 - b) Label and write the ordered pair of the vertex. What does this mean in real life?
 - c) Label and write the ordered pairs of the roots/zeros. What do these points mean in real life?
- 2. The graph below shows the height of a toy rocket after it is launched.
 - a) How many seconds is the rocket in the air?
 - b) What math concept did you use to determine this?
 - c) What is the maximum height of the rocket?
 - d) At what time does the maximum height occur?
 - e) At what times is the rocket 120 meters above the earth?



f) Complete the table of values below with first and second differences.

Time	Height	First Diff	Second Diff
0			
1			
2			
3			
4			

g) What pattern did you observe in the second differences from the table? How does this prove that the relationship is quadratic?

6.10.2 Applying Quadratic Relationships

There are many relationships that turn out to be quadratic. One of the most common is the relationship between the height of something (or someone) flying through the air and time.

- 1. A football player kicks a ball of a football tee. The height of the ball, *h*, in metres after *t* seconds can be modelled using the formula: $h = -5t^2 + 20t$.
 - a) Graph the relationship using your graphing calculator. Remember that you need to set your window settings. Record the window settings you used.
 - b) Sketch your graph in the window at right. Make sure to label your axes.

- c) You can get the table of values for this relationship. Press 2nd and WINDOW to access the table setup screen. Make sure your screen looks like the one given.
- d) Now press [2nd] and [GRAPH]. Fill in the window with the values you see.
- e) For which times does the height not make sense? Why?
- f) What is the initial height of the ball?
- g) Where do you look in the table and the graph to determine the answer?
- h) Why does this make sense?



SETUP

Ask

Ask

WINDOW

⟨min=

Xmax= Xscl=

'min=

Ymax=

Yscl= Xres=

TABLE

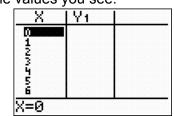
TblStar

⊿Tbl=1

Indent:

Depend:





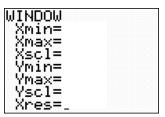
6.10.2 Applying Quadratic Relationships (continued)

- i) What is the maximum height of the ball?
- j) Where do you look in the table and the graph to determine the answer?
- k) When does the ball hit the ground? _____
- I) Where do you look in the table and the graph to determine the answer?
- m) When is the ball more 10 m above the ground? (You may need to give approximate answers.)

Playing Football on Mars

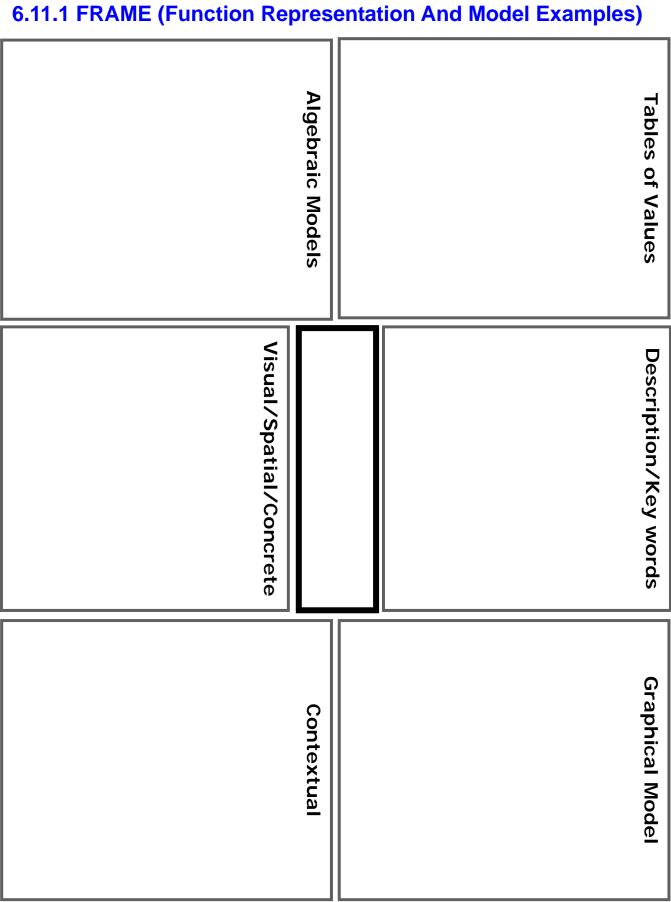
2. The force of gravity on Mars is less than half that on Earth. A ball thrown upward can be modelled using $h = -2t^2 + 15t + 2$ where *h* is the height in m and *t* is the time in seconds.

 a) Graph the relationship using your graphing calculator. Remember that you need to set your window settings. Record the window settings you used. You may need to play around with the settings until you see the full graph.



- b) What is the initial height of the ball? _____
- c) Explain what this means.
- d) What is the maximum height of the ball?
- e) When does the ball reach its maximum height?
- f) When does the ball hit the ground?
- g) When is the ball more 20 m above the ground? (You may need to give approximate answers.)
- h) If the same ball was thrown upward on the Earth, how would you expect the relationship to change?
- i) The force of gravity on Jupiter is much greater than on the Earth. If the same ball was thrown upward on Jupiter, how would you expect the relationship to change?

Unit 6 Day 11	Unit 6 Day 11 : Review of Quadratics				
Minds On: 10 M	Minds On: 10 Min. Math Learning Goals • Demonstrate ability to accurately apply quadratics lessons from the unit		Materials		
Action: 60 Mi Consolidate/ Debrief: 5 Min Total = 75 Min	<u>n.</u>		graphing calculator BLM 6.11.1 BLM 6.11.2 BLM 6.11.3 (teaching notes) BLM 6.11.4		
	Ass		ment unities		
Minds On	Whole Class – Review		unities		
	Review the key concepts and processes for quadratics. Use FRAME organizer (BLM 6.11.1) to consolidate ideas and concepts for review.		Prepare a few key examples for students to look at and place in the frame model.		
		N	Students reflect on their learning to		
Action!	Groups of 2-3 – Game Students are placed into groups of 2-3 and are given an envelope with the first question in it. When they complete the first question, they come to the front of the class and pick another envelope and so on until the entire package is done. They can pick the order of questions that they do but all groups need to successfully complete all questions.		come up with ideas for each section of the FRAME model. Encourage students to look through their notes and examples.		
	Mathematical Processes/Tool & Strategies/Checklist : Circulate around the class to ensure students have recalled the tools & strategies necessary to solve a quadratics problem OR debrief with the group before they receive their next question.		Game questions are on BLM 6.11.2. Teacher solution is on BLM 6.11.3.		
Consolidate Debrief	Groups of 2-3 - Self-Reflection/Discussion Distribute BLM 6.11.4 - Students should take a few minutes at the end of class to discuss their team efforts as well as what skills they're doing well at and what skills they still need to work on based on the review activity.		It may be beneficial to refer students to a list of skills and concepts on the board or a word wall to answer questions 3 and 4.		
Application Concept Practice Reflection Skill Drill	Home Activity or Further Classroom Consolidation Assign additional review questions or give a practice assessment to students to complete.				



6.11.2 Review of Quadratics

1. Linear vs Quadratic

- A linear relation forms a graph with a _____.
- A quadratic relation forms a graph with shape of a ______.
- Below is a table of value, determine if this relation is linear, quadratic or neither:

Time (x)	Distance (v)		
	(y)	First	
		Differences	Second
			Difference

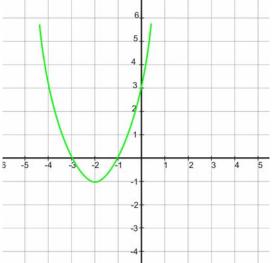
The relation is:		

- A linear relation has the _____equal and the _____equal to _____
- A quadratic relation has the ______ equal.

6.11.2 Review of Quadratics (Continued)

2. Features of a Quadratic Graph					
 A quadratic relation can be seen when a ball is thrown in the air and the height is measured versus time. A sketch of this graph might look: 	 A quadratic relation can be seen when a duck flies into the water, catches a fish and flies back out: 				
This parabola is facing and the vertex is a	This parabola is facing and the vertex is a				

• The key features of a quadratic graph are:



6.11.2 Review of Quadratics (Continued)

3. Forms of A Quadratic - Standard Form: $y = ax^2 + bx + c$

- The y-intercept is the _____ or ____ term. •
- We can change factored into standard form by ______. There are three methods of expanding: ______, ____, and ______,
- Example 1: Find the y-intercept, x-intercepts of the following quadratic:

$$y = (x + 4)(x - 5)$$

Method 1: Tiles	Method 2: Table	Method 3: Algebra (FOIL)

The y-intercept is: _____ and _____

Example 2: Expand the following: y = 2x(3x - 4)

6.11.2 Review of Quadratics (Continued)

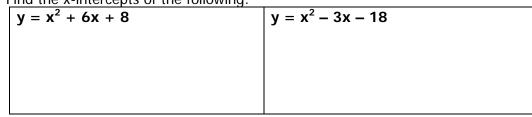
4. Forms of A Quadratic - Factored Form: y = (x - r)(x - s)

- There are two methods of factoring: algebra tiles and algebra
- Example: factor $\mathbf{y} = \mathbf{x}^2 + 3\mathbf{x} + 2$ using tiles

				0	
			-		
		_		_	
_					
_				_	
				_	
_		-			\square

1. <u>Product/Sum Form: Factor $y = ax^2 + bx + c$ </u>

- In this case $r \times s = c$ and r + s = b
- Find the x-intercepts of the following:



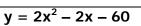
2. Common Factoring: $y = ax^2 + bx$

 Let us factor: y = x² + 3x This can be written as:
 Based on this r × s = _____
 r + s =

The factored form is y =_____

• Factor as state the x and y intercepts of:

$$y = x^2 + 6x$$



_____ or ____

3. Difference of Squares: $y = ax^2 - b^2$

- y = x² 4 can be written as y = _____
 r × s = _____
 - r + s = factored form

$$y = x^2 - 16$$
 $y = 2x^2 - 200$

6.11.3 Review of Quadratics- Teacher

1. Linear vs Quadratic

- A linear relation forms a graph with a <u>straight line</u>.
- A quadratic relation forms a graph with shape of a <u>parabola</u>.
- Below is a table of value, determine if this relation is linear, quadratic or neither:

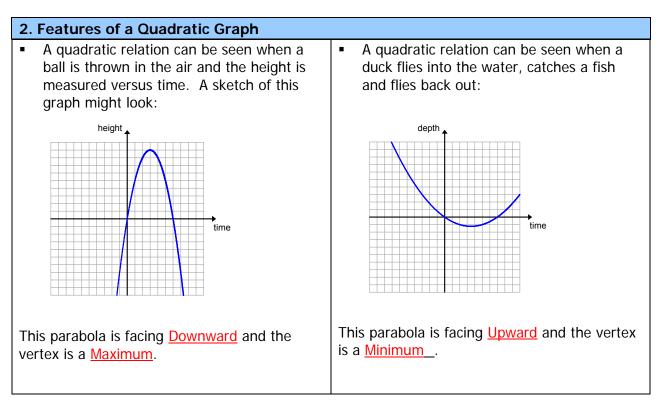
Time (x)	Distance (y)		
		First	
0	2	Differences	Second
-		1	Difference
1	3		2
		3	2
2	6		2
		5	2
3	11		
4	18	/	
4	10		-

The relation is:

Quadratic since the second differences are the same.

- A linear relation has the <u>first differences</u> equal and the <u>second differences</u> equal to <u>zero</u>.
- A quadratic relation has the <u>second differences</u> equal.

6.11.3 Review of Quadratics - Teacher (Continued)



6.11.3 Review of Quadratics -Teacher (Continued)

3. Forms of A Quadratic - Standard Form: $y = ax^2 + bx + c$

- The y-intercept is the <u>last</u> or <u>c</u> term.
- We can change factored into standard form by <u>expanding</u>.
- There are three methods of expanding: <u>Algebra Tiles</u>, <u>Table Method</u>, and <u>Algebra (FOIL)</u>.
- Example 1: Find the y-intercept, x-intercepts of the following quadratic:

Method 1: TilesMethod 2: TableMethod 3: Algebra (FOIL)
$$x$$
 x $+4$ x x x x^2 x

The y-intercept is: -20The x-intercepts are: -4 and 5.

Example 2: Expand the following: y = 2x(3x - 4) $y = 6x^2 - 8x$

y = (x + 4)(x - 5)

6.11.3 Review of Quadratics - Teacher (Continued)

4. Forms of A Quadratic - Factored Form: y = (x - r)(x - s)

- There are two methods of factoring: algebra tiles and algebra
- Example: factor $\mathbf{y} = \mathbf{x}^2 + 3\mathbf{x} + 2$ using tiles

		-	

1. <u>Product/Sum Form: Factor $y = ax^2 + bx + c$ </u>

- In this case r × s = c and r + s = b
- Find the x-intercepts of the following:

$y = x^2 + 6x + 8$ 2 + 4 = 6	$y = x^2 - 3x - 18$ 3 + (-6) = -3
$2 \times 4 = 8$	3 × (-6) = -18
y = (x + 2)(x + 4)	y = (x + 3)(x - 6)
x-intercepts are -2 and -4	x-intercepts are -3 and 6

2. Common Factoring: $y = ax^2 + bx$

- Let us factor: $y = x^2 + 3x$ This can be written as: $y = x^2 + 3x + 0$ Based on this $r \times s = 0$ r + s = 3The factored form is y = (x + 0)(x + 3) or x(x + 3).
- Factor as state the x and y intercepts of:

$y = x^{2} + 6x$	$y = 2x^2 - 2x - 60$		
= x(x + 6)	= 2(x ² - x - 30)		
x-intercepts 0, -6 y-intercept 0	= 2(x + 5)(x - 6) x-intercepts -5, 6 y-intercept -60		

3. Difference of Squares: $y = ax^2 - b^2$

```
• y = x^2 - 4 can be written as y = x^2 + 0x - 4

r \times s = -4

r + s = 0 factored form y = (x + 2)(x - 2)

y = x^2 - 16

= (x + 4)(x - 4)

y = 2x^2 - 200

= 2(x^2 - 100)

= 2(x - 10)(x + 10)
```

6.11.4 Review of Quadratics - Reflection

After you've completed the review activity, answer the following questions in your group. If your answer involves circling a number, note that 5 is really well and 1 is poor.

1.	Rate your contribution to your team's efforts. (5 is the best rating, 1 is the poorest)
	1 2 3 4 5
_	
2.	Rate your team-mate's contribution. (5 is the best rating, 1 is the poorest) 1 2 3 4 5
3.	Identify 2 areas of quadratics that you did really well at:
4.	Identify 2 areas of quadratics that you need to work on a bit more:
5.	What concept(s) would you like to have explained to you again?
1	

6.11.5 My Notes